

# SIMILARITY...

## Trigonometry

### What do I need to be able to do?

By the end of this unit you should be able to:

- Work fluently with hypotenuse, opposite and adjacent sides
- Use the tan, sine and cosine ratio to find missing side lengths
- Use the tan, sine and cosine ratio to find missing angles
- Calculate sides using Pythagoras' Theorem

### Keywords

**Enlarge:** to make a shape bigger (or smaller) by a given multiplier (scale factor)

**Scale Factor:** the multiplier of enlargement

**Constant:** a value that remains the same

**Cosine ratio:** the ratio of the length of the adjacent side to that of the hypotenuse. The sine of the complement

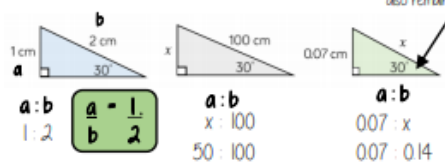
**Sine ratio:** the ratio of the length of the opposite side to that of the hypotenuse.

**Tangent ratio:** the ratio of the length of the opposite side to that of the adjacent side.

**Inverse:** function that has the opposite effect.

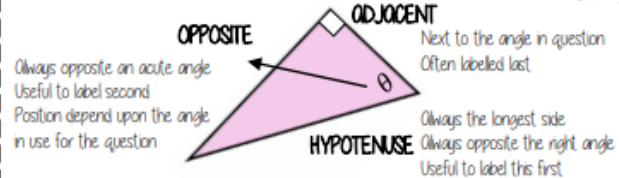
**Hypotenuse:** longest side of a right-angled triangle. It is the side opposite the right-angle.

### Ratio in right-angled triangles



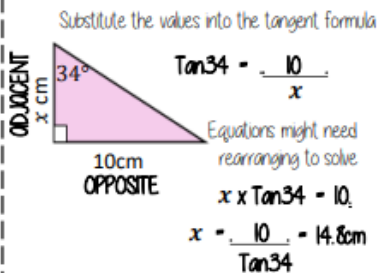
### Hypotenuse, adjacent and opposite

ONLY right-angled triangles are labelled in this way



### Tangent ratio: side lengths

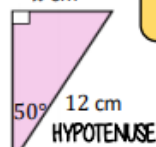
$$\tan \theta = \frac{\text{opposite side}}{\text{adjacent side}}$$



### Sin and Cos ratio: side lengths

OPPOSITE  
x cm

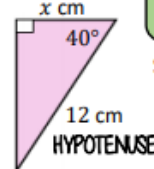
$$\sin \theta = \frac{\text{opposite side}}{\text{hypotenuse side}}$$



NOTE  
The Sin(x) ratio is the same as the Cos(90-x) ratio

ADJACENT  
x cm

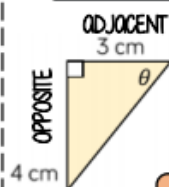
$$\cos \theta = \frac{\text{adjacent side}}{\text{hypotenuse side}}$$



Substitute the values into the ratio formula  
Equations might need rearranging to solve

### Sin, Cos, Tan: Angles

#### Inverse trigonometric functions



Label your triangle and choose your trigonometric ratio

Substitute values into the ratio formula

$$\tan \theta = \frac{3}{4}$$

$$\theta = \tan^{-1} \frac{3}{4}$$

$$\theta = 36.9^\circ$$

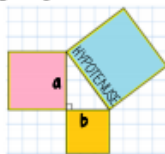
$$\theta = \tan^{-1} \frac{\text{opposite side}}{\text{adjacent side}}$$

$$\theta = \sin^{-1} \frac{\text{opposite side}}{\text{hypotenuse side}}$$

$$\theta = \cos^{-1} \frac{\text{adjacent side}}{\text{hypotenuse side}}$$

### Pythagoras theorem

$$\text{Hypotenuse}^2 = a^2 + b^2$$



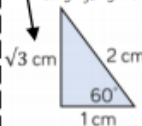
This is commutative - the square of the hypotenuse is equal to the sum of the squares of the two shorter sides

Places to look out for Pythagoras

- Perpendicular heights in isosceles triangles
- Diagonals on right angled shapes
- Distance between coordinates
- Any length made from a right angles

### Key angles

This side could be calculated using Pythagoras



$$\tan 30 = \frac{1}{\sqrt{3}}$$

$$\tan 60 = \sqrt{3}$$

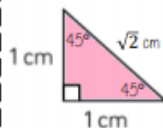
$$\cos 30 = \frac{\sqrt{3}}{2}$$

$$\cos 60 = \frac{1}{2}$$

$$\sin 30 = \frac{1}{2}$$

$$\sin 60 = \frac{\sqrt{3}}{2}$$

Because trig ratios remain the same for similar shapes you can generalise from the following statements



$$\tan 45 = 1$$

$$\cos 45 = \frac{1}{\sqrt{2}}$$

$$\sin 45 = \frac{1}{\sqrt{2}}$$

### Key angles 0° and 90°

$$\tan 0 = 0$$

This value cannot be defined - it is impossible as you cannot have two 90° angles in a triangle

$$\sin 0 = 0$$

$$\sin 90 = 1$$

$$\cos 0 = 1$$

$$\cos 90 = 0$$

