

PROPORTION...

Ratios and fractions

What do I need to be able to do?

By the end of this unit you should be able to:

- Compare quantities using ratio
- Link ratios and fractions and make comparisons
- Share in a given ratio
- Link Ratio and scales and graphs
- Solve problems with currency conversions
- Solve 'best buy' problems
- Combine ratios

Keywords

Ratio: a statement of how two numbers compare

Equivalent: of equal value

Proportion: a statement that links two ratios

Integer: whole number, can be positive, negative or zero

Fraction: represents how many parts of a whole

Denominator: the number below the line on a fraction. The number represents the total number of parts.

Numerator: the number above the line on a fraction. The top number. Represents how many parts are taken

Origin: (0,0) on a graph. The point the two axes cross

Gradient: The steepness of a line

Compare with ratio R

'For every dog there are 2 cats'



The ratio has to be written in the same order as the information is given

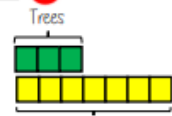
eg 2:1 would represent 2 dogs for every 1 cat

Units have to be of the same value to compare ratios

Ratios and fraction R

Trees: Flowers

3:7



Fraction of trees

Number of parts of in group / Total number of parts = $\frac{3}{10}$

Ratio

Fraction

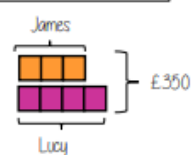
Sharing a whole into a given ratio R

James and Lucy share £350 in the ratio 3:4
Work out how much each person earns

Model the Question

James: Lucy

3:4



Find the value of one part

Whole: £350

7 parts to share between (3 James, 4 Lucy)

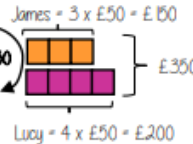
$$£350 \div 7 = £50$$

□ = one part = £50

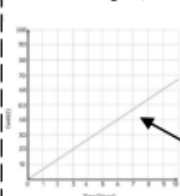
Put back into the question

James: Lucy

$\times 50$ 3:4 $\times 50$
£150:£200



Ratio and graphs R



Graphs with a constant ratio are directly proportional

- Form a straight line
- Pass through (0,0)

The gradient is the constant ratio

Ratio and scale R

A picture of a car is drawn with a scale of 1:30

The car image is 10cm

Image: Real life
1cm: 30cm
 $\times 10$ 10cm: 300cm $\times 30$



Conversion between currencies R

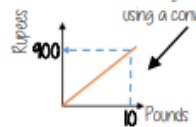
£1 = 90 Rupees

Currency is directly proportional

For every £1 I have 90 Rupees

$\times 10$ £1 = 90 Rupees
 $\times 10$ £10 = 900 Rupees

Currency can be converted using a conversion graph



Convert 630 Rupees into Pounds

$\times 7$ £1 = 90 Rupees
 $\times 7$ £7 = 630 Rupees

Ratios in 1:n and n:1

This is asking you to cancel down until the part indicated represents 1

Show the ratio 4:20 in the ratio of 1:n

The question states that this part has to be 1 unit. Therefore Divide by 4

$\frac{4:20}{4:5}$
 $\frac{1:5}$

This side has to be divided by 4 too - to keep in proportion

the n part does not have to be an integer for this type of question

Best buys

4 pens costs £2.60 10 pens costs £6.00

1 pen costs... £2.60 ÷ 4 = **£0.65**

1 pound buys... 4 ÷ 2.60 = **1.54 pens**

10 pens costs £6.00 £6.00 ÷ 10 = **£0.60**

10 ÷ 6 = **1.67 pens**

You could work out how much 40 pens are and then compare.

Compare the solution in the context of the question

The best value has the lowest cost 'per pen'

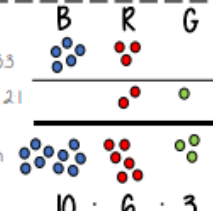
The best value means £1 buys you more pens

Combining ratios

The ratio of Blue counters to Red counters is 5:3

The ratio of Red counters to Green counters is 2:1

Ratio of Blue to Red to Green



Use equivalent ratios to allow comparison of the group that is common to both statements

Lowest common multiple of the ratio both statements share