

# GEOMETRY...

## Angles and bearings

### What do I need to be able to do?

By the end of this unit you should be able to:

- Understand and represent bearings
- Measure and read bearings
- Make scale drawings using bearings
- Calculate bearings using angle rules
- Solve bearings problems using Pythagoras and trigonometry

### Keywords

**Cardinal directions:** the directions of North, South, East, West

**Angle:** the amount of turn between two lines around their common point

**Bearing:** the angle in degrees measured clockwise from North

**Perpendicular:** where two lines meet at  $90^\circ$

**Parallel:** straight lines always the same distance apart and never touch. They have the same gradient.

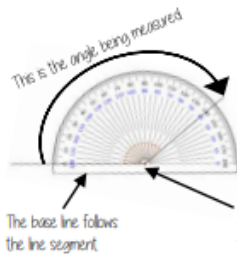
**Clockwise:** moving in the direction of the hands on a clock.

**Construct:** to draw accurately using a compass, protractor and/or ruler or straight edge.

**Scale:** the ratio of the length of a drawing to the length of the real thing

**Protractor:** an instrument used in measuring or drawing angles

### Measure angles to $180^\circ$

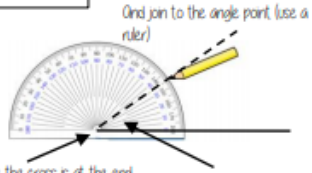


Read from  $0^\circ$  on the base line. Remember to use estimation. This is an obtuse angle so between  $90^\circ$  and  $180^\circ$ .

Make sure the cross is at the point the two lines meet.

### Draw angles up to $180^\circ$

Draw a  $35^\circ$  angle



The angle

### Angle notation

The letter in the middle is the angle. The arc represents the part of the angle.



**Angle Notation:** three letters:  $ABC$ . This is the angle at  $B = 113^\circ$ .  $\angle ABC$  is also used to represent the angle at  $B$ .

### Scale drawings

1:20

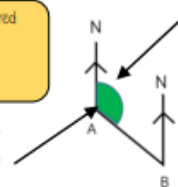
For every 1cm on the model there are 20cm in real life.

Remember: Scale drawings **ONLY** change lengths and distances. Angles remain the same.

### Understand and represent bearings

- A bearing is always measured from **NORTH**
- It is always given as three figures

The bearing of  $B$  from  $A$  is calculated by measuring the highlighted angle.



The angle indicated starts from the North line at  $A$  and joins the path connecting  $A$  to  $B$ .

This angle shows the bearing of  $B$  from  $A$ .

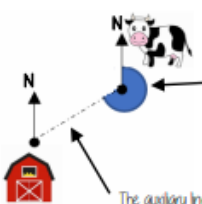
The sentence... "Bearing of \_\_\_ from \_\_\_" is really important in identifying the bearing being represented.

Using **estimation** it is clear this angle is between  $090^\circ$  and  $180^\circ$ .

### Directions



### Measure and read bearings



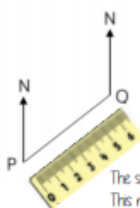
The bearing of the cow to the barn

This angle is measured from **NORTH**. It is measured in a clockwise direction. **Estimation** indicates this angle is between  $180^\circ$  and  $270^\circ$ . Use a protractor to measure accurately. Remember bearings are written as three figures.

The auxiliary line is drawn to help you measure and draw the angle that is measured to represent the bearing.

### Scale drawings using bearings

Remember — angles **DO NOT** change size in scaled drawings.



The bearing measurements do not change from "real life" to images.

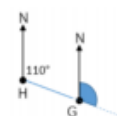
The units in the ratio scale are the same.

The scale may need to be calculated from the image. This represents 30km from  $P$  to  $Q$ .

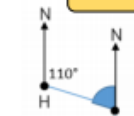
6cm = 30km  
6:30,000,000

### Bearings with angle rules

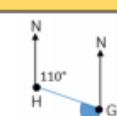
Because two North lines are **PARALLEL**...



They form **corresponding angles** and therefore are the same size.



They form **co-interior angles** and add up to  $180^\circ$ .



They form **alternate angles** and therefore are the same size.

### Bearings with right-angled geometry

"Due West" bearing of  $270^\circ$  makes a  $90^\circ$  angle.

"Due East" bearing of  $090^\circ$  makes a  $90^\circ$  angle.

Look for Right-angles Pythagoras Trigonometry (Sin, Cos, Tan)

Q plane flies East for 20km then turns South for 15km. Find the bearing of the plane from where it took off.

